## Quick Introduction

- born and raised in Germany
- moved to United States when I was 16
- 1998-2004: PhD at the University of Illinois, Urbana-Champaign
- dissertation research on statistical methods for meta-analysis
- at the time, the meta-analytic landscape in R looked like this ...

Wolfgang Viechtbauer
Maastricht University
2019-05-31

## Early Developments

- 1993: RevMan released (not R) [1]
- 1997: MetaWin released (also not R) [2]
- 1998: Comprehensive Meta-Analysis released (still no R) [3]
- 1999: rmeta package, but no 'meta-regression' capabilities
- ~2000: wrote function for fitting random/mixed-effects models
- ~2005: put function on my personal website
- ~2005: meta package (still no meta-regression)
- 2006-2009: a few other packages
- 2009: published metafor package
- 2009-2019: lots of new packages (current count: 107)
based on CRAN Task View on Meta-Analysis: https://cran.r-project.org/view=MetaAnalysis


## CRAN Task View: Meta-Analysis

CRAN Task View: Meta-Analysis
Maintainer: Michael Dewey
Contact: lists at dewey.myzen.co.uk
Version: 2019-05-06
URL: https://CRAN.R-project.org/view=MetaAnalysis
This task view covers packages which include facilities for meta-analysis of summary statistics from primary studies. The task view does not consider the meta-analysis of individual participant data (IPD) which can be handled by any of the standard linear modelling functions but does include some packages which offer special facilities for IPD.

The standard meta-analysis model is a form of weighted least squares and so any of the wide range of R packages providing weighted least squares would in principle be able to fit the model. The advantage of using a specialised package is that (a) it takes care of the small tweaks necessary (b) it provides a range of ancillary functions for displaying and investigating the model. Where the model is referred to below it is this model which is meant.

Where summary statistics are not available a meta-analysis of significance levels is possible. This is not completely unconnected with the problem of adjustment for multiple comparisons but the packages below which offer this, chiefly in the context of genetic data, also offer additional functionality.

## First Releases of Meta-Analysis Packages



Exponential Growth (sort of)


## Development of the metafor Package

- first version (0.5-0) released 2009-06-04
- a total of 28 versions released so far
- latest is 2.1-0 released 2019-05-13
- added various illustrative datasets over the years (35 as of now)
- added various outcome measures over the years ( 60 as of now)
- full changelog:
https://wviechtb.github.io/metafor/news/index.html


## Some Milestones

| Version | Date | Notes / Changes |
| :---: | :---: | :---: |
| 0.5-0 | 2009-06-04 | - first version released on CRAN <br> -rma.uni(), rma.mh(), rma.peto() |
| 0.5-4 | 2009-09-18 | - regtest() and ranktest() functions <br> - anova() function |
| 0.5-5 | 2009-10-08 | - cumul () and leave1out () functions |
| 0.5-7 | 2009-12-06 | - permutest() function |
| 1.0-1 | 2010-02-02 | - version 1 released |
| 1.4-0 | 2010-07-30 | - various improvements for JSS paper |
|  | 2010-08-05 | - JSS paper published |
| 1.5-0 | 2010-12-16 | - started metafor website |
|  |  | - labbe () function |

## Some Milestones

| Version | Date | Notes / Changes |
| :---: | :---: | :---: |
| 1.9-8 | 2015-09-28 | - robust () function |
|  |  | - confint () works for rma.mv objects |
| 1.9-9 | 2016-09-25 | - started using git and GitHub |
|  |  | - ranef () and gosh () functions |
|  |  | - permutation-based Cls of model coefficients |
| 2.1-0 | 2019-05-13 | - vif () and reporter () functions |
|  |  | - cluster-level outlier/influence statistics |
|  |  | - more parallel processing |
|  |  | - continuous time autoregressive structures |
|  |  | - spatial correlation structures |
| 2.2-0 | devel | - phylogenetic correlation structures |

## Some Milestones

| Version | Date | Notes / Changes |
| :---: | :---: | :---: |
| 1.7-0 | 2013-02-06 | - rma.glmm() function |
| 1.9-0 | 2013-06-21 | - hc() function |
| 1.9-1 | 2013-07-20 | - baujat() function |
| 1.9-2 | 2013-10-07 | - rma.mv() and profile() functions |
| 1.9-3 | 2014-05-05 | - models with user-defined weights |
|  |  | - sparse matrices for rma.mv () |
|  |  | - autoregressive structures for rma.mv() |
| 1.9-4 | 2014-07-30 | - generalized Q-statistic estimator of $\tau^{2}$ |
| 1.9-6 | 2015-05-07 | - multiple correlated random effects |
|  |  | - parallel processing for profile() |

## Lines of Code



Lines of Code vs Game of Thrones Viewers


## Package Features: Effect Sizes and Outcome Measures

- measures for $2 \times 2$ table data (e.g., RD, RR, OR)
- measures for two-group person-time data (e.g., IRR, IRD)
- raw/standardized mean differences and response ratios
- conversions of $2 \times 2$ table data / ORs to SMDs and vice-versa
- raw and Fisher's r-to-z transformed correlation coefficients
- (semi)partial correlations and biserial/tetrachoric correlations
- proportions and transformations thereof
- incidence rates and transformations thereof
- raw/standardized mean change measures
- measures of change in $2 \times 2$ table data
- reliability measures (Cronbach's alpha and transformations)
- measures that quantify variability (and group differences thereof)


## Package Features: Models and Analysis Approaches

## Package Features: Plots and Figures

- fixed-, random-, and mixed-effects (meta-regression) models
- Mantel-Haenszel and Peto's (one-step) method
- generalized linear (mixed-effects) models
- multilevel and multivariate meta-analytic models
- network meta-analysis / mixed treatment comparisons
- phylogenetic meta-analysis
- spatio-temporal meta-analytic models
- models with user-defined weights
- forest plots
- funnel plots
- Baujat plots
- L'Abbé plots
- radial (Galbraith) plots
- GOSH plots
- profile likelihood plots
- normal quantile-quantile plots


## Package Features: Publication Bias

- rank correlation test
- Egger's regression test
- trim and fill method
- Henmi and Copas approach
- file drawer analysis


## Package Features: Inference Methods

- likelihood ratio and Wald-type tests
- Knapp and Hartung method
- confidence intervals for heterogeneity statistics
- permutation tests / confidence intervals
- (cluster) robust tests and confidence intervals
- cumulative meta-analysis
- best linear unbiased predictions
- model fit / information criteria criteria
- bootstrapping (via boot package)
- multimodel inference (via glmulti and MuMIn packages)
- multiple imputation (via mice package)
- raw, standardized, and studentized residuals
- DFFITS, DFBETAS values, Cook's distances, covariance ratios
- cluster-level outlier/influence statistics
- model weights and hat values
- leave-one-out analyses

https://wviechtb.github.io/metafor/articles/pkgdown/diagram.html


## Demo: Random-Effects Model

| library (metafor) |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \#\#\# look at BCG dataset dat.bcg |  |  |  |  |  |  |  |  |
| \#\# | trial | author year | tpos | tneg | cpos | cneg | ablat | alloc |
| \#\# 1 | 1 | Aronson 1948 | 4 | 119 | 11 | 128 | 44 | random |
| \#\# 2 | 2 | Ferguson \& Simes 1949 | 6 | 300 | 29 | 274 | 55 | random |
| \#\# 3 | 3 | Rosenthal et al 1960 | 3 | 228 | 11 | 209 | 42 | random |
| \#\# 4 | 4 | Hart \& Sutherland 1977 | 62 | 13536 | 248 | 12619 | 52 | random |
| \#\# 5 | 5 | Frimodt-Moller et al 1973 | 33 | 5036 | 47 | 5761 | 13 | alternate |
| \#\# 6 | 6 | Stein \& Aronson 1953 | 180 | 1361 | 372 | 1079 | 44 | alternate |
| \#\# 7 | 7 | Vandiviere et al 1973 | 8 | 2537 | 10 | 619 | 19 | random |
| \#\# 8 | 8 | TPT Madras 1980 | 505 | 87886 | 499 | 87892 | 13 | random |
| \#\# 9 | 9 | Coetzee \& Berjak 1968 | 29 | 7470 | 45 | 7232 | 27 | random |
| \#\# 10 | 10 | Rosenthal et al 1961 | 17 | 1699 | 65 | 1600 | 42 | systematic |
| \#\# 11 | 11 | Comstock et al 1974 | 186 | 50448 | 141 | 27197 | 18 | systematic |
| \#\# 12 | 12 | Comstock \& Webster 1969 | 5 | 2493 | 3 | 2338 | 33 | systematic |
| \#\# 13 | 13 | Comstock et al 1976 | 27 | 16886 | 29 | 17825 | 33 | systematic |

## Demo: Random-Effects Model

```
### random-effects model (using log risk ratios and variances as input)
res <- rma(yi, vi, data=dat)
res
## Random-Effects Model ( }\textrm{k}=13\mathrm{ ; tau^2 estimator: REML)
##
## tau^2 (estimated amount of total heterogeneity): 0.3132 (SE = 0.1664)
## tau (square root of estimated tau^2 value): 0.5597
## I~2 (total heterogeneity / total variability): 92.22%
## H^2 (total variability / sampling variability): 12.86
##
## Test for Heterogeneity:
## Q(df = 12) = 152.2330, p-val < .0001
##
## Model Results
##
## estimate se zval pval ci.lb ci.ub
## -0.7145 0.1798
```


## Demo: Random-Effects Model

\#\#\# calculate log risk ratios and corresponding sampling variances dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, data=dat.bcg) dat

| \#\# | trial | author year | yi | i |
| :---: | :---: | :---: | :---: | :---: |
| \#\# 1 | 1 | Aronson 1948 | -0.8893 | 0.3256 |
| \#\# 2 | 2 | Ferguson \& Simes 1949 | -1.5854 | 0.1946 |
| \#\# 3 | 3 | Rosenthal et al 1960 | -1.3481 | 0.4154 |
| \#\# 4 | 4 | Hart \& Sutherland 1977 | -1.4416 | 0.0200 |
| \#\# 5 | 5 | Frimodt-Moller et al 1973 | -0.2175 | 0.0512 |
| \#\# 6 | 6 | Stein \& Aronson 1953 | -0.7861 | 0.0069 |
| \#\# 7 | 7 | Vandiviere et al 1973 | -1.6209 | 0.2230 |
| \#\# 8 | 8 | TPT Madras 1980 | 0.0120 | 0.0040 |
| \#\# 9 | 9 | Coetzee \& Berjak 1968 | -0.4694 | 0.0564 |
| \#\# 10 | 10 | Rosenthal et al 1961 | -1.3713 | 0.0730 |
| \#\# 11 | 11 | Comstock et al 1974 | -0.3394 | 0.0124 |
| \#\# 12 | 12 | Comstock \& Webster 1969 | 0.4459 | 0.5325 |
| \#\# 13 | 13 | Comstock et al 1976 | -0.0173 | 0.0714 |

## Demo: Random-Effects Model

```
### then do lots more stuff
forest(res)
funnel(res)
influence(res)
plot(influence(res))
leave1out(res)
baujat(res)
ranktest(res)
regtest(res)
trimfill(res)
funnel(trimfill(res))
cumul(res)
forest(cumul(res))
radial(res)
labbe(res)
plot(gosh(res))
# note: the following plots are based on various datasets
```

Demo: Forest Plot
Author(s) and Year
Aronson, 1948
Ferguson \& Simes, 1949
Rosenthal et al, 1960
Hart \& Sutherland, 1977
Frimodt-Moller et al, 1973

Demo: Funnel Plot


## Demo: Contour-Enhanced Funnel Plot



## Demo: Outlier / Influence Diagnostics



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## Demo: Baujat Plot



## Demo: Trim-and-Fill



Demo: Cumulative Meta-Analysis

| Author(s) and Year |
| :--- | :--- | :--- |
| Aronson, 1948 |
| + Ferguson \& Simes, 1949 |
| + Stein \& Aronson, 1953 |
| + Rosenthal et al, 1960 |
| + Rosenthal et al, 1961 |
| + Coetzee \& Berjak, 1968 |
| + Comstock \& Webster, 1969 |

Demo: Radial (Galbraith) Plot


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## Demo: L’Abbé Plot



## Demo: GOSH Plot



Demo: Meta-Regression
\#\#\# mixed-effects meta-regression model
res <- rma(yi, vi, mods = ~ ablat + alloc, data=dat)
res

```
## Mixed-Effects Model (k = 13; tau^2 estimator: REML)
##
## tau^2 (estimated amount of residual heterogeneity): 0.1446 (SE = 0.1124)
## tau (square root of estimated tau^2 value): 0.3803
## I^2 (residual heterogeneity / unaccounted variability): 70.11%
## H^2 (unaccounted variability / sampling variability): 3.35
## R^2 (amount of heterogeneity accounted for): 
##
## Test for Residual Heterogeneity:
## QE(df = 9) = 26.2034, p-val = 0.0019
##
## .
```

res <- rma(yi, vi, mods = ~ ablat + alloc, data=dat)

Demo: Meta-Regression

```
##
## Test of Moderators (coefficients 2:4)
## QM(df = 3) = 11.0605, p-val = 0.0114
##
## Model Results:
##
# estimate se zval pval ci.lb ci.ub
## intrcpt }\begin{array}{lllllll}{0.2932}&{0.4050}&{0.7239}&{0.4691}&{-0.5006}&{1.0870}
## ablat -0.0273 0.0092 -2.9650}00.0030 -0.0453 -0.0092
## allocrandom 
## allocsystematic }\begin{array}{lllllll}{0.0585}&{0.3795}&{0.1540}&{0.8776}&{-0.6854}&{0.8023}
```

Demo: Forest Plot with Subgroups

|  | Vaccinated |  | $\mathrm{TB}_{+}^{\text {Control }}{ }_{\text {TB- }}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Author(s) and Year | TB+ | TB- |  |  |  |  |  | Risk Ratio [95\% Cl] |
| Systematic Allocation |  |  |  |  |  |  |  |  |
| Comstock et al, 1976 | 27 | 16886 | 29 | 17825 |  |  | - | 0.98 [0.58, 1.66] |
| Comstock \& Webster, 1969 | 5 | 2493 | 3 | 2338 |  |  |  | $1.56[0.37,6.53]$ |
| Comstock et al, 1974 | 186 | 50448 | 141 | 27197 |  |  | - | $0.71[0.57,0.89]$ |
| Rosenthal et al, 1961 | 17 | 1699 | 65 | 1600 |  | $\square$ |  | $0.25[0.15,0.43]$ |
| RE Model for Subgroup $\left(\mathrm{Q}=16.59, \mathrm{df}=3, \mathrm{p}=0.00 ; \mathrm{I}^{2}=86.4 \%\right.$ ) |  |  |  |  |  |  |  | $0.65[0.32,1.32]$ |
| Random Allocation |  |  |  |  |  |  |  |  |
| $\begin{array}{lllll}\text { Coetzee \& Berjak, } 1968 & 29 & 7470 & 45 & 7232\end{array}$ |  |  |  |  |  |  |  | 0.63 [0.39, 1.00] |
|  |  |  |  |  |  |  |  | 1.01 [0.89, 1.14] |
|  |  |  |  |  |  |  |  | 0.20 [0.08, 0.50] |
| $\begin{array}{llllll}\text { Hart \& Sutherland, } 1977 & 62 & 13536 & 248 & 12619\end{array}$ |  |  |  |  |  |  |  | 0.24 [0.18, 0.31] |
| Rosenthal et al, 1960   <br> Ferguson \& Simes. 1949 3  |  |  |  |  |  |  |  | 0.26 [0.07, 0.92] |
|  |  |  |  |  |  |  |  | $0.20[0.09,0.49]$ |
|  |  |  |  |  |  |  |  | $0.41[0.13,1.26]$ |
| RE Model for Subgroup ( $\mathrm{Q}=110.21, \mathrm{df}=6, \mathrm{p}=0.00 ; 1^{2}=89.9 \%$ ) |  |  |  |  |  |  |  | 0.38 [0.22, 0.65] |
| Alternate Allocation |  |  |  |  |  |  |  |  |
| Stein \& Aronson, 1953 Frimodt-Moller et al, 1973 | 180 | 1361 | 372 | 1079 |  |  |  | $0.46[0.39,0.54]$ |
|  | 33 | 5036 | 47 | 5761 |  |  |  | 0.80 [0.52, 1.25] |
| RE Model for Subgroup ( $\mathrm{Q}=5.56, \mathrm{df}=1, \mathrm{p}=0.02 ; \mathrm{r}^{2}=82.0 \%$ ) |  |  |  |  |  |  |  | 0.58 [0.34, 1.01] |
| RE Model for All Studies ( $\mathrm{Q}=152.23, \mathrm{df}=12, \mathrm{p}=0.00 ; \mathrm{I}^{2}=92.2 \%$ ) |  |  |  |  |  |  |  | 0.49 [0.34, 0.70] |
|  |  |  |  |  | 0.05 | 0.25 | 1 |  |
|  |  |  |  |  |  | Risk | Ratio |  |

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Demo: Meta-Analytic Scatterplot


## The reporter () Function

- automatically generates a report based on rma. uni objects
- describes the statistical methods used
- gives a natural language summary of the results
- includes a forest and a funnel plot
- gives references for all methods used
- output can be html, pdf, or docx


## To-Do for reporter ()

- make reporter () work with meta-regression models
- other ideas:
- option to suppress/customize forest/funnel plots
- allow transformation of results (e.g., log risk ratio to risk ratio)
- add explanatory footnotes
- more customization (group names, outcome name, ...) - extend to rma.mh, rma.peto, and rma.glmm objects


## Quick Demo: Using reporter ()

dat <- escalc(measure="RR", ai=tpos, bi=tneg, ci=cpos, di=cneg, slab=paste(author, ", ", year, sep=""), data=dat.bcg)
res <- rma(yi, vi, data=dat)
reporter(res)

Directory for generating the report is: /tmp/RtmpfH6xxC
Copying references.bib and apa.csl to report directory ...
Saving model object to report_res.rdata ...
Creating report_res.rmd file ...
Rendering report_res.rmd file ...
Generated /tmp/RtmpfH6xxC/report_res.html ...
Opening report ...

## Impact: Downloads

- not possible to track total downloads across all CRAN mirrors
- can get counts for the RStudio CRAN mirror (Oct 2012 - now)
- roughly 244 k downloads in total


Impact: Citations

- Viechtbauer, W. (2010). Conducting meta-analyses in R with the metafor package. Journal of Statistical Software, 36(3), 1-48.
- Citations: WoS Core Collection: 2968 / Google Scholar: 4282



## Impact: Tools that makes use of metafor

- CRAN packages: bayesmeta, hetmeta, metaforest, metawho, SAMURAI, catmap, concurve, ConfoundedMeta, eefAnalytics, EValue, fmri, getmstatistic, ggstatsplot, KenSyn, mc.heterogeneity, meta, metagear, metagen, metamedian, metamisc, metaplus, MetaUtility, metaviz, NSM3, psychmeta, PublicationBias, puniform, RcmdrPlugin.MA, Replicate, reproducer, rma.exact, SimTimeVar, SSDforR, xmeta, ...
- OpenMeta \& OpenMEE (Center for Evidence Synthesis in Health)
- metaforGUI
- jamovi + MAJOR and JASP
- metaBUS and MetaLab
- ...

Impact: Disciplines


## Support

- documentation, documentation, documentation



## Email Support $\rightarrow$ Mailing List



Validation / Testing

- extensive comparisons with other R/software packages
- comparison with published results (e.g., analysis examples)
- testing via simulation studies
- appreciable user base
- automated testing + code coverage ( $\sim 70 \%$ )


## Philosophy

- build a toolbox, not individuals tools
- try to avoid special cases
- coherent and general modeling framework; e.g., rma.mv () for:
- multilevel meta-analysis (e.g., [4], website)
- multivariate meta-analysis (e.g., [5], website)
- network meta-analysis (e.g., example 1, example 2)
- phylogenetic meta-analysis (e.g., [6], [7])
. spatio-temporal models (e.g., [8])
- figure out logical generalizations
- listen to users


## The Future

- keep expanding on the capabilities
- add location-scale models to rma.uni ()
- add selection models to rma. uni () (and rma.mv () ?)
- allow fitting rma. uni () models using fully Bayesian methods
- make reporter() work with meta-regression models
-...
- a meta-analysis data package (metadat) - in progress!


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- add location-scale models to rma.uni()
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- allow fitting rma. uni () models using fully Bayesian methods
- make reporter() work with meta-regression models
- ...
- a meta-analysis data package (metadat) - in progress!
- ...
- rewrite everything from scratch!


## References ii

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Thank You!
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